Singletons and You

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Preface

Slide available at https://talks.jle.im/lambdaconf-2017/singletons/singleton-slides.html.

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GHC extensions (potentially) used:

| {-# | LANGUAGE | GADTs | #-} |
|-----|----------|----------------------|-----|
| {-# | LANGUAGE | KindSignatures | #-} |
| {-# | LANGUAGE | LambdaCase | #-} |
| {-# | LANGUAGE | RankNTypes | #-} |
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| {-# | LANGUAGE | ScopedTypeVariables | #-} |
| {-# | LANGUAGE | TemplateHaskell | #-} |
| {-# | LANGUAGE | TypeFamilies | #-} |
| {-# | LANGUAGE | TypeInType | #-} |
| {-# | LANGUAGE | TypeOperators | #-} |
| {-# | LANGUAGE | UndecidableInstances | #-} |
| | | | |

import Data.Kind -- to get type Type = *
import Data.Singletons

```
data DoorState = Opened | Closed | Locked
  deriving (Show, Eq)
```

data Door (s :: DoorState) = UnsafeMkDoor

```
-- alternatively
data Door :: DoorState -> Type where
UnsafeMkDoor :: Door s
```

Other similar examples

- State machines (socket connections, file handles, opened/closed)
- Refinement types
- "Tagged" types (santized/unsantized strings)

Phantom types in action

closeDoor :: Door 'Opened -> Door 'Closed
closeDoor UnsafeMkDoor = UnsafeMkDoor

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```
openDoor :: Door 'Closed -> Door 'Opened
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```

Phantom types in action

```
doorStatus :: Door s -> DoorState
doorStatus = -- ????
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More Problems

```
initalizeDoor :: DoorStatus -> Door s
initializeDoor = \case
    Opened -> UnsafeMkDoor
    Closed -> UnsafeMkDoor
    Locked -> UnsafeMkDoor
```

More Problems

```
initalizeDoor :: DoorStatus -> Door s
initializeDoor = \case
    Opened -> UnsafeMkDoor
    Closed -> UnsafeMkDoor
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```

Neat, but does this work?

More Problems

ghci> :t initializeDoor Opened :: Door 'Closed initializeDoor Opened :: Door 'Closed

Oops.

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- This is a good thing for performance! Types incur no runtime overhead!
- But it makes functions like doorStatus fundamentally unwritable without fancy typeclasses.
- ... or does it?

data SingDS :: DoorStatus -> Type where
 SOpened :: SingDS 'Opened
 SClosed :: SingDS 'Closed
 SLocked :: SingDS 'Locked

Creates three constructors:

| SOpened | :: | SingDS | 'Opened |
|---------|----|--------|---------|
| SClosed | :: | SingDS | 'Closed |
| SLocked | :: | SingDS | 'Locked |

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- There is only one value of type SingDS 'Opened, and only one value of type SingDS 'Closed.
- The constructor that a SingDS s uses reveals to us what s is.

With our new singletons, we can essentially **pattern match** on types:

showSingDS :: SingDS s -> String
showSingDS = \case
 SOpened -> "Opened"
 SClosed -> "Closed"
 SLocked -> "Locked"

With our new singletons, we can essentially **pattern match** on types:

showSingDS :: SingDS s -> String
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 SOpened -> "Opened"
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Alone like this, it's a bit boring. We didn't need GADTs for this.

Door Status

doorStatus' :: SingDS s -> Door s -> DoorState
doorStatus' = \case
 SOpened -> _ -> "Door is opened"
 SClosed -> _ -> "Door is closed"
 SLocked -> _ -> "Door is locked"

 GADT-ness allows us to enforce that the s in SingDS s is the same as the s in our Door.

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- Singleton property means that SingDS s has a one-to-one correspondence with its constructors.

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- GADT-ness allows us to enforce that the s in SingDS s is the same as the s in our Door.
- Singleton property means that SingDS s has a one-to-one correspondence with its constructors.
- Pattern matching on that single constructor reveals to us the type of Door.

Implicit Passing

```
class SingDSI s where
    singDS :: SingDSI s
```

```
instance SingDSI 'Opened where
    singDS = SOpened
instance SingDSI 'Closed where
    singDS = SClosed
instance SingDSI 'Locked where
    singDS = SLocked
```

Implicit Passing

```
class SingDSI s where
    singDS :: SingDSI s
```

```
instance SingDSI 'Opened where
    singDS = SOpened
instance SingDSI 'Closed where
    singDS = SClosed
instance SingDSI 'Locked where
    singDS = SLocked
doorStatus :: SingDSI s => Door s -> DoorState
doorStatus = doorStatus' singDS
```

Implicit Passing

```
class SingDSI s where
    singDS :: SingDSI s
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```
instance SingDSI 'Opened where
    singDS = SOpened
instance SingDSI 'Closed where
    singDS = SClosed
instance SingDSI 'Locked where
    singDS = SLocked
doorStatus :: SingDSI s => Door s -> DoorState
doorStatus = doorStatus' singDS
ghci> doorStatus (UnsafeMkDoor :: Door 'Locked)
Door is locked!
```

```
initializeDoor' :: SingDS s -> Door s
initializeDoor' _ _ = UnsafeMkDoor
```

Initialize Door

initializeDoor' :: SingDS s -> Door s
initializeDoor' _ _ = UnsafeMkDoor

ghci> :t initializeDoor' SOpened initializeDoor SOpened :: Door 'Opened ghci> :t initializeDoor' SClosed initializeDoor SClosed :: Door 'Closed

```
Implicit passing style:
```

```
initializeDoor :: SingDSI s => Door s
initializeDoor = initializeDoor' singDS
```



- Really, SingDS s -> is the same as SingDSI s =>
- The two are the same way of providing the same information to the compiler, and at runtime.

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- The two are the same way of providing the same information to the compiler, and at runtime.
- We can use the two styles interchangebly.
- One is explicitly passing the type, the other is explicitly passing the type.

Sometimes we don't care about what the status of our door is, and we want the type system to relax.

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This is essentially the same as saying that the status of our door is a runtime property that we do not want to (or sometimes can't) check at compile-time.

Ditching the phantom

data SomeDoor :: Type where MkSomeDoor :: SingDS s => Door s -> SomeDoor

Ditching the phantom

```
data SomeDoor :: Type where
    MkSomeDoor :: SingDS s => Door s -> SomeDoor
ghci> let myDoor = MkSomeDoor (initializeDoor SOpened)
ghci> :t myDoor
myDoor :: SomeDoor
ghci> case myDoor of MkSomeDoor d -> doorStatus d
Door is opened.
```

Runtime-deferred types

initializeSomeDoor :: DoorStatus -> SomeDoor initializeSomeDoor = \case Opened -> SomeDoor (initialiseDoor' SOpened) Closed -> SomeDoor (initialiseDoor' SClosed) Locked -> SomeDoor (initialiseDoor' SLocked)

Runtime-deferred types

```
initializeSomeDoor :: DoorStatus -> SomeDoor
initializeSomeDoor = \case
    Opened -> SomeDoor (initialiseDoor' SOpened)
    Closed -> SomeDoor (initialiseDoor' SClosed)
    Locked -> SomeDoor (initialiseDoor' SLocked)
ghci> let myDoor = initializeSomeDoor Locked
ghci> :t myDoor
myDoor :: SomeDoor
ghci> case myDoor of MkSomeDoor d -> doorStatus d
Door is locked.
```

The Singletons Library

The singletons library provides a unified framework for creating and working with singletons for different types (not just DoorStatus), and also for functions on those types.

http://hackage.haskell.org/package/singletons

The singletons way

```
$(singletons [d|
  data DoorState = Opened | Closed | Locked
  deriving (Show, Eq)
  |])
```

The singletons way

```
$(singletons [d|
  data DoorState = Opened | Closed | Locked
  deriving (Show, Eq)
  |])
```

This creates three types and three constructors:

```
-- not the actual code, but essentially what happens
data Sing :: DoorState -> Type where
SOpened :: Sing 'Opened
SClosed :: Sing 'Closed
SLocked :: Sing 'Locked
```

Sing is a poly-kinded type constructor (family):

The singletons way

And also

```
instance SingI 'Opened where
   sing = SOpened
instance SingI 'Closed where
   sing = SClosed
instance SingI 'Locked where
   sing = SLocked
```

(SingI is a poly-kinded typeclass)

Examples

```
STrue :: Sing 'True
SJust SFalse :: Sing ('Just 'True)
SOpened `SCons` SClosed `SCons` SNil :: Sing '[ 'Opened, 'O
ghci> sing :: Sing 'True'
STrue
```

Other stuff created from the library

Some other convenient features:

```
ghci> fromSing SOpened
Opened
ghci> let s = toSing Opened
ghci> it s
```

```
ghci> :t s
```

```
s :: SomeSing DoorStatus
```

ghci> case s of

SomeSing SOpened -> "Opened." SomeSing SClosed -> "SClosed." SomeSing SLocked -> "SLocked."

Non-trivial type logic

```
knock :: Door s -> IO ()
knock = -- ??
```

We want to allow the user to knock on a closed or locked door, but not an opened door.

```
knock :: Door s -> IO ()
knock = -- ??
```

We want to allow the user to knock on a closed or locked door, but not an opened door.

We can do this simple case using pattern matching, but it's not always feasible or scalable. We want to define a type relationship that can be used by potentially many functions.

```
$(singletons [d|
  canKnock :: DoorState -> Bool
  canKnock Opened = False
  canKnock Closed = True
  canKnock Locked = True
  |])
```

```
$(singletons [d]
canKnock :: DoorState -> Bool
canKnock Opened = False
canKnock Closed = True
canKnock Locked = True
]])
knock :: (CanKnock s ~ True) => Door s -> IO ()
knock _ = putStrLn "knock knock!"
```

```
$(singletons [d]
  canKnock :: DoorState -> Bool
  canKnock Opened = False
  canKnock Closed = True
  canKnock Locked = True
  11)
knock :: (CanKnock s ~ True) => Door s -> IO ()
knock = putStrLn "knock knock!"
ghci> knock (initializeDoor SOpened)
Compile Error!!!!
ghci> knock (initializeDoor SClosed)
knock knock!
```

```
tryKnock' :: Sing s -> Door s -> IO ()
tryKnock' s = case sCanKnock s of
   STrue -> knock
   SFalse -> \_ -> putStrLn "Cannot knock door!"
tryKnock :: SingI s => Door s -> IO ()
tryKnock = tryKnock' sing
```

```
tryKnock' :: Sing s \rightarrow Door s \rightarrow IO ()
tryKnock' s = case sCanKnock s of
    STrue -> knock
    SFalse -> \ -> putStrLn "Cannot knock door!"
tryKnock :: SingI s => Door s \rightarrow IO ()
tryKnock = tryKnock' sing
ghci> tryKnock (initializeDoor SOpened)
Cannot knock door!
ghci> tryKnock (initializeDoor SClosed)
knock knock!
```

Vectors

```
$(singletons [d|
data N = Z | S N
]])
data Vec :: N -> Type -> Type where
VNil :: Vec Z a
(:*) :: a -> Vec n a -> Vec (S n) a
```

infixr 5 :*

The Types demand it

```
replicateV'
    :: Sing n
    -> a
    -> Vec n a
replicateV' = \case
    SZ    -> \_ -> VNil
    SS n   -> \x -> x :* replicateV' n x
```

The Types demand it

```
replicateV'
    :: Sing n
    -> a
    \rightarrow Vec n a
replicateV' = \case
    SZ -> \ -> VNil
    SS n \rightarrow x \rightarrow x := replicateV' n x
replicateV
    :: SingI n
    => a
    -> Vec n a
replicateV = replicateV' sing
```

Thank you!

Further confusion: https://blog.jle.im/entry/verified-instances-in-haskell.html